## Surgical Planning and Biomechanical Analysis

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Overview - Surgical Planning



## Region Growing

- Joined regions
- Undetected regions


## Fuzzy Connectivity

- The weakest link in the strongest path



## Segmentation - Post Processing

- Remove possible noise
- Fill holes
- Morphological operations
- Dilate
- Errode
- Opening
- Closing



## Surface Generation



1. Use the Segmented volume and create a triangle mesh of the surface

2. Simplify geometry

## Contour following



Segmented image


Contour points

## Contour Simplification

- Collinear points are deleted
- Only the first and the last is kept
- Maximum distance as parameter of the simplification



## Contour Simplification



All contour points before simplification


After simplification

## 2D contour reconstruction

- Bernhard Geiger (INRIA) : NUAGES
- Input: a set of simple closed polygons on parallel planes
- Output: 3D surface




## Marching Squares I.

- Marching Squares (2D)
- 16 configurations


23

## Marching Cubes

- Fully 3D
-256 situations
- generalized in 15 families by rotations and symetries



## Marching Cubes II.




## Surface Simplification Methods

- Vertex Decimation

- Edge Collapse
- Vertex Clustering

- Face Merging


28

## Vertex Decimation

- Schroeder et al, 92
- Based on controlled removal of vertices
- Loop
- choose a removable vertex $v$
- delete $v$ and its incident faces
- re-triangulate the hole
- Until
- no more removable vertex exists or reduction rate fulfilled



## Vertex Decimation

- Vertex is removable iff
- Distance to average plane is lower than $\mathrm{e}_{\max }$
- Distance to boundary is lower than $\mathrm{e}_{\text {max }}$
- Properties

- Efficient
- Simple implementation \& use
- Works on large meshes
- Implemented in VTK
d: distance to plane



## Edge Collapse

- Examine all vertex pairs
- Build queue of edges or $\mathrm{V}_{1}, \mathrm{~V}_{2}$ pairs where

$$
\left\|\vec{V}_{1}-\vec{V}_{2}\right\|<t
$$

- Loop
- Take edge e from the queue with the least error
- Delete e and its triangles
- Update queue
- Until
- Queue is empty or target reduction reached


## Edge Collapse

- Error of a vertex is the sum of squared distances to its planes
- Position of the new vertex is where the vertex error is minimal



## Vertex Clustering

- Object's bounding box is subdivided into a grid
- All vertices inside a cell are clustered to one representative vertex
- Layout of the grid controls the simplified model
- Properties
- Very fast
- Poor quality
- No direct controll of reduction rate



## Co-planar face merging

- Kalvin, Taylor '96
- Partitions the surface into connected disjoint co-planar regions
- Regions are replaced by a polygon
-Polygon boundary is simplified
- Boundary retriangulated


Repositioning with the Mouse


Repositioning - Heptic device

http://www.sensable.com/index.htm

## Surgical Planning

- Treat bone surfaces as objects in 3D space
- Transformations
- Translation
- Rotation
- Implants
- Screw
- Fixation Plate


39

## Surgical Planning

- 3D object positioning requires learning
- The model is 3D but the screen and the mouse is 2 D
- Collision detection can help
- Automatic tool is needed


## Repositioning using Registration

- Semi-automatic: user selects surface pairs
- Do registration on every pair one-by one
- Cost function: sum of distances to the nearest neighbours
- Search in 6 dim. space for the minimum of cost function

Collision Detection

$\qquad$



## Properties

- With constraints: good matching of points
- Fast: 5-8 seconds
- BUT: possible errors
- Segmentation
- Simplification
- User input
- Errors accumulate in complex cases



## Complex Fracture



Male, 40Y, 7 fragments

Pairwise Surface Registration



## Global Optimization

- All surface pairs are considered simultaneously
- Search space is $(n-1) * 6$ dim.
- Stronger constraints
- Improves overall result

- Model contains 12 k points
- Points used for registration $2 k-6 k$
- Slow



## Surgical Planning - Fixation Screw

- Screw parameters
- Length
- Insertion depth
- Shank diameter
- Tip length
- Head length/diameter
- Thread length
- Major / minor diameters
- Pitch


## Gethenthtern



## Surgical Planning - Fixation Plate

- Fixation plate
- Width
- Height
- Length
- Follow surface



Surgical Plan - Example II.


Surgical Plan - Example II.


## Stress

- Stress is a measure of the internal distribution of force per unit area within a body that balances and reacts to the loads applied to it.
$F$ : force,
A: crossectional area
$\sigma=F / A$

- Unit: $\mathrm{N} / \mathrm{m}^{2}=\mathrm{Pa}$


## Strain

Strain is the geometrical expression of deformation caused by the action of stress

$$
\varepsilon=\Delta \mathrm{L} / \mathrm{L}
$$

$L$ : original length
$\Delta L$ : change in length
Unit: no unit


## Deformation

- Elastic region: the deformation is proportional to the force
- Plastic region: the material undergoes a non-reversible change



## Hooke's law

- Hooke's law (1676): $F$, is proportional to $u$ by a constant factor, $k$
$F=k u$


F
WWM-
Where, $k$ is the spring constant, $u$ stretching distance

- Elastic materials: $E$ is the elastic modulus.

$$
\sigma=\mathrm{E}_{\varepsilon}
$$

- Generalised to 3D by Cauchy

$$
\begin{aligned}
& {\left[\begin{array}{c}
\sigma_{\mathrm{xx}} \\
\sigma_{\mathrm{yy}} \\
\sigma_{z z} \\
\sigma_{\mathrm{yz}} \\
\sigma_{\mathrm{zx}} \\
\sigma_{\mathrm{xy}}
\end{array}\right]} \\
& \text { Stress } \\
& \text { Stress }
\end{aligned}
$$

$t 1$

Hooke's law

## Hooke's law

- Izotropic material: the material properties are independent of direction (2 elastic constants)

- Ortotropic material: 2-3 orthogonal planes of symmetry, where material properties are independent of direction within each plane
- Anisotropyc (21 elastic constants)


## Young's modulus

- Modulus of elasticity
- The slope of the stressstrain curve
$\mathrm{E}=\sigma / \varepsilon$
- SI unit: Pa

| Material | E (GPa) |
| :--- | ---: |
| Diamond | 1200 |
| Steel | 210 |
| Iron | 196 |
| Aluminium | 69 |

## Poisson's ratio

- Defined as the ratio of the contraction strain normal to the applied load divided by the extension strain in the direction of the applied load
- $\mathrm{n}=-\varepsilon_{\text {trans }} / \varepsilon_{\text {longitud }}$
- $-1<=\mathrm{n}<0.5$

| Rubber | 0.495 |
| :--- | :--- |
| Steel | 0.28 |
| Bone | 0.3 |
| Cork | 0.0 |

## Negative Poisson's Ratio Materials



## Finite Element Method

- If we can not solve the original problem, let's brake it into smaller, but well known pieces and solve it that way!

$K=2 \mathrm{r} \pi$

$\mathrm{K}_{\mathrm{n}}=\mathrm{nK}_{\mathrm{ij}}$
$\mathrm{K}_{\mathrm{ij}}=\mathrm{K}_{45}=2 \mathrm{r} \sin (\pi / \mathrm{n})$
$\pi_{\mathrm{n}}=\mathrm{K}_{\mathrm{n}} / 2 \mathrm{r}=\mathrm{n}$



## Finite Element Mesh

- The model is a mesh of springs
- Nodes define the geometry
- Elements define which nodes are connected



## Element library I.

- Primitive elements

Real
Rod element

Pipe element

Arbitrary profil

## Element library II.

- Shell elements: 2D, but with thickness

Real


## Triangle

Quadrangle

Discrete


## Element library III.

- 3D elements


Hexahedron

How an engineer works


How an engineer works



How an engineer works


How an engineer works


Loaded area is marked with red arrows

How an engineer works


Generation of the finite element mesh

How an engineer works


How an engineer works


## Irregular objects

- There is no CAD model of the patients broken bone
- No automatic mesh generation
- Fixed points and loaded areas



## Mechanical Model

- Geometrical model
- Nodes
- Finite elements (shell, tetra, hexa)
- Material properties (Young's modulus, Poisson' ratio)
- Load
- Boundary conditions
- Connections between objects

Load and boundary conditions



## Mechanical Model Generation



- Ul for Load and BC
- Mesh generation
- Shell elements
- Solid (tetra-, hexahedron) elements
- Quadtree / Octree
- Advancing Front
- Delaunay


## Mechanical Model Shell Elements

- Based on the geometry $\rightarrow$ 3-node shell el.
- Relation between objects $\rightarrow 2$-node el.

- Start with bounding box
- Recursively build quadtree



## Mechanical Model Generation



## Octree/Quadtree

Intersection Point


- Triangulate Intersection, Side, and Corner Points



## Advancing Front



- Bundary is the initial front
- Process front segments
- Calculate ideal position for triangle


## Advancing Front



- Check radius around optimal node for existing front nodes


## Advancing Front



- Delete orig. front elements and insert new ones
- Continue while front exists



## Advancing Front



- Delete orig. front elements and insert new ones
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## Advancing Front



- In case of multiple possibilities, chose best quality



## Bowyer-Watson algoritmusa



Iteratively insert new points

1. Find all triangles whose circumcircle contains the new node.
2. Remove edges interior to these triangles
3. Connect nodes of this empty space to new node.



Example II. - Pelvis



Example IV. - Jaw

## Conclusion

- Results match to the clinical expectations
- Quantitative comparative measurements still pending
- Possible Applications
- Clinical practice
- Education
- Navigation
- Research


